

Evaluate the following limits. Write "DNE" if a limit does not exist.

SCORE: ____ / 11 PTS

You do not need to show the use of the limit laws. However, it must be clear how you got your answers.

$$\begin{aligned}
 \text{[a]} \quad \lim_{x \rightarrow 3} \frac{x^3 - 6x + 9}{x^2 + 2x - 3} &= \frac{27 - 18 + 9}{9 + 6 - 3} \\
 &= \frac{18}{12} = \frac{3}{2}
 \end{aligned}$$

$$\text{[b]} \quad \lim_{x \rightarrow -4} f(x) \text{ if } f(x) = \begin{cases} \sqrt[3]{x-4}, & \text{if } x < -4 \\ 0, & \text{if } x = -4 \\ \frac{x}{x+6}, & \text{if } x > -4 \end{cases}$$

$$\lim_{x \rightarrow -4^+} f(x) = \lim_{x \rightarrow -4^+} \frac{x}{x+6} = \frac{-4}{2} = -2 \text{ (1)}$$

$$\lim_{x \rightarrow -4^-} f(x) = \lim_{x \rightarrow -4^-} \sqrt[3]{x-4} = \sqrt[3]{-8} = -2 \text{ (1)}$$

$$\lim_{x \rightarrow -4} f(x) = -2 \text{ (1)}$$

$$\begin{aligned}
 \text{[c]} \quad \lim_{x \rightarrow 5} \frac{x-5}{3-\sqrt{2x-1}} \cdot \frac{3+\sqrt{2x-1}}{3+\sqrt{2x-1}} &= \lim_{x \rightarrow 5} \frac{(x-5)(3+\sqrt{2x-1})}{9-(2x-1)} \\
 &= \lim_{x \rightarrow 5} \frac{(x-5)(3+\sqrt{2x-1})}{-2x+10} \text{ (1/2)} \\
 &= \lim_{x \rightarrow 5} -\frac{3+\sqrt{2x-1}}{2} \text{ (1)} \\
 &= -\frac{6}{2} = -3 \text{ (1)}
 \end{aligned}$$

$$\begin{aligned}
 \text{[d]} \quad \lim_{x \rightarrow -2} \frac{1+\frac{2}{x}}{\frac{6}{4+x}-3} \cdot \frac{x(4+x)}{x(4+x)} &= \lim_{x \rightarrow -2} \frac{x(4+x)+2(4+x)}{6x-3x(4+x)} \\
 &= \lim_{x \rightarrow -2} \frac{(x+2)(4+x)}{3x(-x-2)} \text{ (1/2)} \\
 &= \lim_{x \rightarrow -2} -\frac{4+x}{3x} \text{ (1)} \\
 &= -\frac{2}{-6} = \frac{1}{3} \text{ (1)}
 \end{aligned}$$

Prove that $\lim_{x \rightarrow 0} x^4 \sin \frac{1}{x^2} = 0$.

SCORE: _____ / 4 PTS

① $-1 \leq \sin \frac{1}{x^2} \leq 1$ FOR ALL $x \neq 0$

① $-x^4 \leq x^4 \sin \frac{1}{x^2} \leq x^4$

① $\lim_{x \rightarrow 0} -x^4 = 0 = \lim_{x \rightarrow 0} x^4$

SO BY SQUEEZE THEOREM, $\lim_{x \rightarrow 0} x^4 \sin \frac{1}{x^2} = 0$

①
②

③
④

The graph of f is shown on the right. Evaluate the following limits. Write "DNE" if a limit does not exist.

SCORE: _____ / 4 PTS

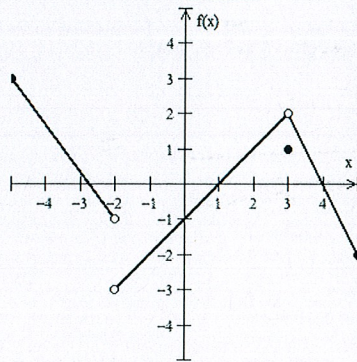
[a] $\lim_{x \rightarrow 3} \frac{x}{5 - 4f(x)}$ ← Show the proper use of
limit laws to find your answer.

[b] $\lim_{x \rightarrow -2^+} f(x)$
 $= \boxed{-3} \text{ (1)}$

$$= \boxed{\frac{\lim_{x \rightarrow 3} x}{\lim_{x \rightarrow 3} 5 - \lim_{x \rightarrow 3} 4 \cdot \lim_{x \rightarrow 3} f(x)}} \text{ (1/2)}$$

$$= \frac{3}{5 - 4 \cdot 2} \text{ (1)}$$

$$= \frac{3}{-3} = \boxed{-1} \text{ (1/2)}$$



SCORE: _____ / 2 PTS

Sketch the graph of an example of a function that satisfies all the following conditions.

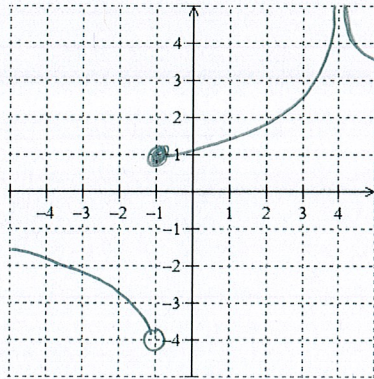
The domain of the function is $[-5, 4) \cup (4, 5]$

$$\lim_{x \rightarrow -1^+} f(x) = 1$$

$$\lim_{x \rightarrow -1^-} f(x) = -4$$

$$\lim_{x \rightarrow 4} f(x) = \infty$$

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Let P be the point on the curve of $f(x) = \sqrt{1-x+3x^2}$ where $x = 3$.

SCORE: _____ / 2 PTS

- [a] If Q is the point on the same curve where $x = b$, write the expression for the slope of the secant line PQ .

$$\frac{\sqrt{1-b+3b^2}-5}{b-3}$$

NOTE: Your answer may use the formula for f , but must not use " $f(\)$ " notation itself.

- [b] Use your calculator to evaluate the slope of 6 appropriate secant lines, then guess the slope of the tangent line at P . Fill in the table below showing the values of b and the corresponding slopes you used to arrive at your answer.

b	Slope of secant line	Slope of tangent line = <u>1.7</u>
<u>3.1</u>	<u>1.7011</u>	
<u>3.01</u>	<u>1.7001</u>	
<u>3.001</u>	<u>1.7</u>	
<u>2.999</u>	<u>1.7</u>	
<u>2.99</u>	<u>1.6999</u>	
<u>2.9</u>	<u>1.6989</u>	

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Use your calculator to evaluate $\lim_{x \rightarrow -1} \frac{2+2x}{x^2 - \sqrt{2x^6 - 1}}$.

SCORE: _____ / 1 PT

Fill in the table below showing the input and output values you used to arrive at your answer.
You must use at least 6 **appropriate** input values.

Input value

Output value

Final answer = 0.5

-1.1

0.51986

-1.01

0.50459

-1.001

0.50005

-0.999

0.49995

-0.99

0.49456

-0.9

0.35763

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